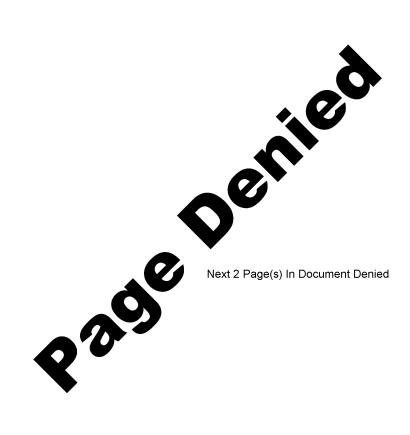
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## COMPUTING CENTRE OF THE USSR ACADEMY OF SCIENCES

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P- 447

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P- 447

MUSIC MOLE FLAR IONS AND
MESIC MOLECULAR PROCESSES IN HYDROGEN



Rivery levels of means motospies are calculated. The numerical alculations were carried out on HESW computer. Corrections due to the motion of auctof up to the first order with respect to \_\_\_\_\_\_ are taken into account.

A special property of mesic avalragem atoms is their neutrality since at distances larger compared to the radius of Bohr mesic atom orbit  $(2.56 \cdot 10^{-11} \text{ cm})$  the nucleus charge is almost completely screened by the meson charge. This concurratorize provides a number of mesic molecular processes in hydrogen (or in the mixture of hydrogen is more such as  $\mathcal{M}$ —meson exchange between various nuclei (charge exchange), formation of mesic molecules etc. These processes define to a large extent the catalysis of nuclear reactions in hydrogen predicted by Frank<sup>1</sup>. Zeldovich<sup>2</sup> and Sacharov<sup>3</sup> and investigated experimentally in papers <sup>1,3</sup>. On the other hand as it was pointed out in <sup>6-8</sup>, mesic molecular processes in (a fragen are important in the experimental determination of the law of interaction  $\mathcal{M} : \mathcal{P} \to \mathcal{A} : \mathcal{K}$  (in particular, in order to distinguish experimentally  $\mathcal{N} = \mathcal{A}$  and  $\mathcal{N} + \mathcal{R}$  forms<sup>3</sup>).

Some mesic molecular processes in by trogen have been studied in earlier papers.

In the paper the levels of mostic molecular some (pp); ; (pd); ; (dd); ; and cross sections of the processes

have been calculated. There is a great discrepancy with our data for the upper level of (  $\operatorname{Id}$ )<sub> $\operatorname{Ar}$ </sub> with  $\operatorname{L} \times 0$ . Our cross section of the solutering of  $\operatorname{Val}$  by protons does not tend to ziro with energy decrease.

In  $^{12}$  the probability of the change exchange  $R_{c} + a + c_{\mu} + P_{c}$  has been calculated by the method similar to that used in the present paper. However, for the potentials  $F_{g}$  and  $F_{u}$  and for the corrections  $R_{gg}$  and  $R_{ug}$  were react functions than those given in  $^{14,15}$  has been taken. Moreover, the authors  $^{12}$  have expected that for  $R \geqslant 6$  the exact solutions of the system coincide with their asymptotic values, what is the quaterninect.

In paper 18 the ground state levels agrees a releasilar ions nave been calculated. The corrections to the potential energy of where  $\frac{1}{4}$  have been neglected. Besides, this in order to find the eigenvalues for mesia make these with different and let we need to solve a system of two equations (owing to the presence of a fine moment of vanish proof a transitions between the states  $\frac{1}{4}$  and  $\frac{1}{4}$  ):

In 20 the levels in mesic more mar toos (pr), and, and a type to determined (the

corrections due to the motiva of an  $N_{\rm c}$  are  $N_{\rm c}$  are  $N_{\rm c}$  and  $N_{\rm c}$  are  $N_{\rm c}$  are then in  $\frac{14}{3}$ .

In paper 19 the estimates of basic levels for me was decular sons at it contions de pare depolare given.

and  $M_2$  and the  $M_1$  -meson, let  $Z_1, Z_2$  be the coordinates of  $M_2$  meson and nuclei. The Hamiltonian stress of  $M_2$  still stress are neglected) is of the form:

$$\hat{\mathcal{H}} = -\frac{1}{2}\Delta_{\mu} = -\frac{1}{2M_1}\Delta_{R_1} - \frac{1}{2M_2}\Delta_{R_2} = \frac{1}{2}, \quad \frac{1}{2}, \quad \frac{1}{2}$$

where

$$z_{i}=/\vec{z}-\vec{R}_{i}/,$$
  $z_{i}=/\vec{z}-\vec{R}_{i}/,$   $R=/\vec{R}_{i}-\vec{R}_{i}/$ 

Believing that the M -meson is on the M -orbit we shall seek for the wave function of the system in the form:

$$\Psi = \omega_{\mathbf{f}}(\mathbf{R}) \Sigma_{\mathbf{g}}(\mathbf{R}, \mathbf{\bar{t}}) + H(\mathbf{R}) \Sigma_{\mathbf{g}} \cdot (\mathbf{R}, \mathbf{\bar{t}})$$
 (2)

where  $\Psi(R)$  and H(R) describe the relative motion of nuclei, and  $\Sigma_g$  and  $\Sigma_n$  represent the wave functions of M meson in the field of fixed nuclei which are from one other at the distance R \*\*. When R —

$$\Sigma_{g} = \frac{1}{\sqrt{2\pi}} \left( e^{-2\epsilon_{i}} \cdot e^{-2\epsilon_{i}} \right), \; \Sigma_{n} = \frac{1}{\sqrt{2\pi}} \left( e^{-2\epsilon_{i}} \cdot e^{-2\epsilon_{i}} \right)$$
 (3)

and where  $R = 0\Sigma_g$  and  $\Sigma_R$  transform into the wave functions of the  $H_e$  ion states 15 and 25 correspondingly.

Substituting (2) into the Schrödinger equation

$$\hat{\mathcal{H}} \varphi = \mathcal{E} \varphi \tag{4}$$

and having in mind that the wave functions  $\Sigma_g$  and  $\Sigma_R$  satisfy the equation:

$$\left(-\frac{1}{2}\Delta z - \frac{1}{z} - \frac{1}{z_2} + \frac{1}{R}\right) \Sigma_i = E_i(R) \Sigma_i(\overline{z}, R) \tag{5}$$

we shall obtain after multiplying by  $\sum_{q}$  and  $\sum_{n}$  and integrating over the M-meson exactinates the system of equations for  $\mathcal{Y}(R)$  and  $\mathcal{H}(R)$ :

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tenest to a /mge = 2.56 10 cm while the most atom units of the most

as het us note that since the wave function (2) depends only on the differences of particle coordinates in the

$$-\frac{1}{2M_{12}} \Delta_{R} \mathcal{A} + \left(E_{g} + \frac{1}{2M_{12}} K_{gg}\right) \mathcal{A} + \frac{1}{2M_{12}} K_{gu} H - \frac{1}{M_{12}} Q_{gu} \nabla_{R} H = E \mathcal{A}$$

$$-\frac{1}{2M_{12}} \Delta_{R} H + \left(E_{u} + \frac{1}{2M_{12}} K_{uu}\right) H + \frac{1}{2M_{12}} K_{ug} \mathcal{A} - \frac{1}{M_{12}} Q_{ug} \nabla_{R} - \mathcal{A} = E H$$
(6)

where  $\frac{1}{M_{12}} = \frac{1}{M_1} + \frac{1}{M_2} = \frac{1}{R} = \frac{1}{R}$ , and the functions  $\frac{1}{2M_{12}} + \frac{1}{M_{12}} + \frac{1}{M_{12}} + \frac{1}{M_{12}} = \frac{1}{M_{12}}$  are the matrix elements between the functions  $\Sigma_g$  and  $\Sigma_u$  of operators

$$\frac{1}{2M_{12}}\hat{\chi} \cdot -\frac{1}{2}\left(\frac{1}{M_1}\Delta\vec{R}_1 + \frac{1}{M_2}\Delta\vec{R}_2\right) \tag{7}$$

$$\frac{1}{M_{LL}}\hat{Q} = \left(-\frac{1}{M}\nabla_{\vec{R}_{\perp}} + \frac{1}{M_{L}}\nabla_{\vec{R}_{\perp}}\right) \tag{8}$$

It is easy to show that due to the normalization conditions of  $\Sigma_q$  and  $\Sigma_u$  the matrix elements of the operator  $\hat{Q}$  are equal zero while the non-diagonal ones are opposite in sign in view of the orthogonality of  $\Sigma_q$  and  $\Sigma_u$ 

$$Q_{gu} = -Q_{ug} = Q \tag{9}$$

If we use the property of symmetry of  $\Sigma_g$  and  $\Sigma \tilde{u}$  with respect to the exchange of nuclei we can depart the dependence on masses in matrix elements

$$\mathbf{A}_{ii} = \int \Sigma_i (-\Delta T_i) \Sigma_i d\tau \qquad i = g, u \tag{10}$$

$$N_{i,j} = \frac{M_{\lambda} - M_{i}}{M_{\lambda} + M_{i}} \int \Sigma_{i} \left( -\Delta \vec{R}_{i} \right) \Sigma_{j} d\tau \tag{11}$$

$$\vec{Q} = \frac{M_2 - M_1}{M_2 - M_1} \left( \Sigma_g \left( - \vec{\nabla}_{\vec{R}} \right) \Sigma_u d\tau = Q \frac{\vec{R}}{R} \right)$$
(12)

Thus, if the nuclei are identical  $M_1 = M_2$  the system of equations (6) breaks up into two independent equations. This result is quite clear since the wave function (2) for identical nuclei in virtue of the symmetry can include only one term (either  $\mathbb{Z}_g$  or  $\mathbb{Z}_{M_1}$ ). The terms represent themselves the corrections to the adiabatic potentials due that of nuclei (with the accuracy up to the first order with respect to  $\mathbb{Z}_{M_2}$ ). Since that of the meson is not so small as for the electron the above terms contribute

essentially. For  $\ell \to \infty$  the value  $Q \to Q$  and the terms  $\frac{1}{2M_{12}} k_{ij}(\infty)$  represent the corrections which take into account the reduced masses of the separated mesic atoms with the accuracy  $(\frac{m_{ij}}{M_1})^2$ ,  $(\frac{m_{ij}}{M_2})^2$ . Noting that the energy of separated mesic atoms (in mesic atom units) is

and taking into account that the matrix elements of the operator  $(-\Delta R_i)$  for  $R \rightarrow \infty$  equal 2 (Assendix) we can write:

$$\left\{ E_{\mathbf{g}}(\boldsymbol{\omega}) \cdot \frac{1}{2H_{\mathbf{h}}} \operatorname{kgg}(\boldsymbol{\omega}) \right\} \left\{ E_{\mathbf{g}}(\boldsymbol{\omega}) \cdot \frac{1}{2H_{\mathbf{h}}} R_{\mathbf{g}\mathbf{g}}(\boldsymbol{\omega}) \right\} = \left( 14 \right)$$

$$Agu = \frac{1}{2M_{12}} Agu = \frac{1}{2} (E_1^* - E_2^*) = \frac{1}{2} \Delta E$$
 (15)

Separating in the quantities  $E_{q}(R), L_{ij}(R)$  and  $\frac{1}{2N_{jk}}K_{ij}(R)$  their values for  $R = \infty$   $E_{q,u}(R) = E_{q,u}(\infty) + E_{q,n}(R)$   $K_{ij}(R) = K_{ij}(\infty) + K_{ij}(R)$ (16)

we sewrite the system of equations (6) in the form

$$\frac{1}{2M_{u}} \Delta R \Psi + (E' + \frac{1}{2M_{u}} N_{gg'}) \Psi + (\frac{1}{2} \Delta E + \frac{1}{2M_{u}} N_{gu}) H - \frac{1}{M_{v}} Q \frac{dH}{dR} =$$

$$\frac{1}{2M_{u}} \Delta_{R} H + (E' + \frac{1}{2M_{u}} N_{uu}) H + (\frac{1}{2} \Delta E + \frac{1}{2M_{u}} N_{ug}) \Psi + \frac{1}{M_{u}} Q \frac{d\Psi}{dR} = E' H$$
(6a)

where  $\Delta E = E^{*}$ ,  $-E^{*}$  and the energy  $E^{*}$  is calculated from the middle between the levels of separated mesic atoms:

$$\mathcal{E}' \cdot \mathcal{E} - \frac{1}{2} \left( \mathcal{E}_{i}^{\bullet} + \mathcal{E}_{k}^{\bullet} \right) \tag{17}$$

When the auclei are identical f' is calculated simply from the level of separate mesic atom). Separating the angular dependence  $\mathcal{I}(R)$  and  $\mathcal{H}(R)$ 

$$9(\overrightarrow{R}) = \frac{1}{R}g_1(R)Y_{L,ML}(\theta,\varphi)$$

$$H_{\epsilon}(\overrightarrow{R}) : \frac{1}{R}h_{\epsilon}(R)Y_{L,ML}(\theta,\varphi)$$

(18)

where (R) is the apherical function) we obtain for g(R) and for h(R) the equations:

(19)

The potentials  $E_g(R)$  and  $E_u(R)$  were determined by solving the Eqs. (5) by many authors, starting with the paper 17. In the present paper the values  $E_g(R)$  and  $E_u(R)$  taken from 14 have been used. The values of the functions k'gg(R) and k'uu(R) may be got by means of the recalculation from 15 and the values G(R), k'ug(R), k'gu(R) are calculated in the approximation of 'united atom' (UA) and 'linear combination of atomic orbits' (LCAO) respectively for small and large values of R (for details see Appendix). For investigating the asymptotic behaviour of the solution for  $R \to \infty$  it is convenient to introduce the functions

Comparing (2) and (3) it is easy to see that the functions u(R) and  $\delta(R)$  for  $R \to \infty$  describe a radial motion of the nucleus with mass  $M_2$  with respect to mesic atom and of the nucleus with mass  $M_1$  with respect to mesic atom with mass respectively  $M_2$ .

The functions (20) satisfy the equations:

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$$\frac{1}{2M_{11}} \left( \frac{1}{2} \frac{1}{2} + \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} \left( \frac{1}{2} \frac{1}{2} + \frac{1}{2} \frac{1}{$$

and the countary condition for R = 0

$$a(0) = b(0) = 0$$
 (22)

Eqs. (21) for A + are of the form:

$$\frac{1}{2N_{LL}} \frac{d^{2}\alpha}{dR^{L}} = \left(E' - \frac{1}{2}\Delta E\right) \cdot Q$$

$$\frac{1}{2N_{LL}} \frac{d^{2}\beta}{dR^{L}} = \left(E' + \frac{1}{2}\Delta E\right) \cdot \beta$$
(23)

Let  $M \notin M_{\mathcal{L}}$  so that for definiteness  $\Delta E > 0$ . Then three types of motion are possible depending on the value of E'.

, i, e. the energy is higher than the K-level of lighter mesic atom. The meson may be near the nucleus  $\mathcal{H}_1$ , as well as near nucleus  $\mathcal{H}_2$ . If at first the meson was near the nucleus  $\mathcal{H}_1$ , and there is charge exchange to the nucleus  $\mathcal{H}_2$ , then it is necessary that the wave functions would obey the following condition: that  $\mathcal{B}(\mathcal{K})$  for  $\mathcal{R} \to \mathcal{C}$  must include only a divergent wave

$$u(R) \approx C_1 e^{iR_1R} + C_2 e^{-iR_1R}$$
 (24)

$$a(R) \approx C_3 e^{-K_2 R}, C_4 e^{-K_2 R}$$
 where  $C_4 = 0$  (25)

b)  $-\frac{1}{2}\Delta E + E' + \frac{1}{2}\Delta E$  i.e. the energy lies between separated mesic atoms. When  $R \rightarrow \infty$  the meson cannot be near the separated lighter nucleus became of lack of energy. This three contributions to the scattering of mesic atom with nucleus  $M_2$  by the nucleus  $M_3$  without the possibility of charge exchange. The wave functions should obey the condition in accordance to which the function  $\alpha(R)$  for  $R \rightarrow \infty$  should not contain an exponentially increasing term:

$$a(R) \simeq \mathfrak{D}_{\ell} e^{-iR_{\ell}R} + \mathfrak{D}_{k} e^{-iR_{\ell}R}$$

$$\mathfrak{D}_{k} = 0$$

$$\delta(R) \simeq \mathfrak{D}_{k} e^{-iR_{k}R} + \mathfrak{D}_{k} e^{iR_{k}R}$$
(26)

$$\mathcal{Z}_{1}^{2} = \mathcal{X}_{1}^{2} = 2M \left( E' - \frac{1}{2} \Delta E \right)$$
 (27)

It is obvious that the conditions (22) and (26) (as well as the conditions (22) and (24) ) can be satisfied at any energy, taken from the considered energy region and determine the solution of the system of equations (21) with the accuracy up to the normalization.

c)  $E'(-\frac{1}{2} \triangle E)$  is a region of the discret spectrum corresponding to the bound states of mesic molecules. For  $R \rightarrow \emptyset$  two conditions are imposed to the solution of the system: the absence of the increasing exponents in both functions a(R) and b(R)

$$a(R) \approx Z_{a} e^{-X_{a}R} + \mathcal{T}_{a} e^{X_{a}R}$$

$$b(R) \approx Z_{a} e^{-X_{a}R} + \mathcal{T}_{a} e^{X_{a}R}$$
(28)

$$\mathcal{F}_{2}(E') = 0$$
,  $\mathcal{F}_{4}(E') = 0$  (29')  
 $\mathcal{F}_{4}^{A} = 2 H_{12} \left( |E'| + \frac{1}{2} \Delta E \right)$ ;  $\mathcal{F}_{2}^{A} = 2 H_{12} \left( |E'| - \frac{1}{2} \Delta E \right)$ 

The conditions (28) and (22) may be satisfied only for definite values of E', being energy translations described the translations and the type (24), (26) and 28) when  $R \rightarrow \infty$  we can find two linear translations astisfying the condition (22) and construct a linear combination section as the translations as the translations as the special point of the second order (16) there exists a connection which can be easily expectated to the second order (16) there exists a connection which can be easily expectated to the second order (16) there exists a connection which can be easily expectated to the second order (16) there exists a connection which can be easily expectated to the second order (16).

ledond, if (3, 11, ) and (2, 1/2) are the solutions of the system (16), then:

For the functions (20), satisfying the condition (22) the indentity (31) takes the form:

$$(a_2 \frac{da_1}{dt} - a_1 \frac{da_2}{dt}) + (b_2 \frac{db_1}{dt} - b_1 \frac{db_2}{dt}) + 2Q(a_1b_2 - a_2b_1) = 0$$
 (32)

The relation (32) may be used for testing the corrections of the numerical integration. As linearly independent solutions for the Eqs. (21) we may choose, for example, the solutions determined for  $R = 0^{\circ}$  by the conditions:

$$\begin{cases} a(0) = b(0) = 0 & g = h = 0 \\ a'(0) = b'(0) = 1 & g' = \sqrt{2}, h' = 0 \end{cases}$$
(33)

$$\begin{cases} a(o) = b(o) = 0 & g = h = 0 \\ a'(o) = -b(o) = 1 & g' = 0; h' = \sqrt{2} \end{cases}$$
 (34)

#### CHARGE EXCHANGE CROSS SECTION

Let in the energy region  $E > \frac{1}{2} \triangle E$  the solutions (20) determined by the conditions (24) and (25) respectively be of the form

Since the functions G(R) and B(R) vanish exponentially incide the potential barriers for R=0 the conditions (88), (84) may be given for numerical integration without canonical error for some small  $R_0 \neq 0$ . In our paper  $R_0 = 0,2$ . This corresponds to the replacement of potentials  $E_0 + \frac{1}{2R_0} R_0$  and  $E_0 + \frac{1}{2R_0} R_0 R_0$ . by the infinite wall at  $R_0 = R_0$ .

$$I \cdot \begin{cases} a_{L}^{(4)} \approx a_{0}^{(1)} \sin \left( \ell, \mathcal{R} \cdot \frac{\mathcal{I}_{L}}{2} + \mathcal{E}_{1} \right) & \underline{H} \\ b_{L}^{(1)} \approx b_{0}^{(1)} \sin \left( \ell \ell, \mathcal{R} \cdot \frac{\mathcal{I}_{L}}{2} + \mathcal{E}_{1} \right) & \\ b_{L}^{(2)} \approx b_{0}^{(2)} \sin \left( \ell \ell_{2} \cdot \mathcal{R} \cdot \frac{\mathcal{I}_{L}}{2} + \mathcal{E}_{2} \right) & \end{cases}$$

$$(35)$$

where constants  $a_o^{(i)}$ ,  $b_o^{(i)}$  are determined by numerical integration of (21). According to (32) there is a connection between the coefficients and the phases of (35)

$$\ell_{1}a_{0}^{(1)}a_{0}^{(2)}$$
 find  $f_{21} + \ell_{1}b_{0}^{(1)}b_{0}^{(2)}$  fin  $\delta_{12} = 0$  (36)

where

$$\int_{2i} - \int_{2}^{\infty} - \int_{i}^{\infty} ; \qquad \delta_{2i} = \delta_{2} - \delta_{i} \tag{37}$$

Forming a linear combination from (35) which satisfies the conditions (33), (34) and the normalization for  $\mathbf{f} \rightarrow \mathbf{e}$  we obtain

for 
$$R \rightarrow \infty$$
 we obtain
$$Q \approx \frac{de^{i(k_1 R - \frac{TL}{L})} - e^{-i(k_1 R - \frac{TL}{L})}}{2iN},$$

$$S \approx \frac{N_1 N_2 \sin \delta}{(N_2 e^{-k_1} - N_2 e^{-if_2 + i\delta})N}. e^{i(k_2 R - \frac{TL}{L} + \delta_2)}$$
(38)

-

$$A_{1} = \frac{\xi_{1}^{\circ}}{Q_{1}^{\circ}}; \quad A_{2} = \frac{\xi_{2}^{\circ}}{Q_{2}^{\circ}}; \qquad Q = \frac{N_{2}e^{-iF_{1}} - N_{1}e^{-iF_{2}} + i\delta^{\circ}}{N_{2}e^{-iF_{1}} - N_{1}e^{-iF_{2}}}; \qquad (39)$$

In accordance with the general theory of inelastic collisions change cross section corresponding to the partial wave L:

the effective charge ex-

$$M_{i}^{2} M_{i}^{2} + \sin^{2} \tilde{Q}_{i} = \frac{d_{2}}{H_{i}^{2} + M_{i}^{2} - 2M_{i}M_{i} \cos (\tilde{Q}_{i} - \tilde{Q}_{i})} \cdot \frac{d_{3}}{H_{i}^{2}}$$
(40)

Constitution can a section

the callicious ecour at a very low energy the scattering in the S state in the most essentiable distance (35) for 4 = 0 take the form :

$$\begin{cases} a_{i}^{(2)} = C_{i}^{(2)} = C_{i}^{(2)}$$

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The three continuity (36) which actisfies the condition (42) and accordingly normalized has

$$anq \cdot \frac{a_6 \cdot r_{a_1} r_{a_2}}{r_{a_1} \cdot r_{a_2} r_{a_2}} b_{a_2} \frac{r_{a_2} r_{a_2} r_{a_2}}{r_{a_1} \cdot r_{a_2} r_{a_2}} \rho^{i(a_2^* q \cdot \delta_2)}$$

$$(43)$$

where

The charge exchange cross section is:

$$G_{pq} = 4\pi \frac{f_{1}^{2}}{f_{1}^{2} + f_{2}^{2} + 2f_{1}f_{2}^{2} \cos \delta_{2l}^{2}} = 4\pi f \alpha_{p}^{2} \frac{V_{1}}{V}$$
(44)

and the electic scattering cross section is

$$G_{ef} = 4\pi \frac{\int_{1}^{R} \int_{2}^{A} + \int_{1}^{r} \int_{2}^{R} - 2T_{1}T_{2} \int_{3}^{R} \int_{2}^{R} \cos \delta_{2d}}{T_{1}^{2} + \Gamma_{2}^{2} - 2T_{1}T_{2} \cos \delta_{2d}} a_{pl}^{2}$$
(46)

If  $V_i$  is the relative velocity of particles,  $N_2$  — the number of nuclei of the isotope with mass  $N_2$  then the probability of the charge exchange is

$$W = N_{A} S_{el} \quad V_{i} = 45 V_{2}^{e} \frac{\Gamma_{i}^{2} \Gamma_{2}^{2} \sin^{2} S_{2i}}{\Gamma_{i}^{2} + \Gamma_{A}^{2} - 2 \Gamma_{i} \Gamma_{2} \cos S_{2i}} \quad \alpha_{ji}^{2} \quad N_{2}$$
 (46)

$$v_{\lambda}^{\bullet} = \sqrt{\frac{2\delta E}{M}}; \quad a_{\mu} = \frac{\hbar^{2}}{m_{\mu}\ell^{\Delta}};$$

The values of v,  $\epsilon_{si}$ , f and  $\epsilon_{si}$  for the systems of proton-deuteron, system preton-tritium and deuteron-tritium are given in Table 1.

## SCATTERING OF HEAVY MESIC ATOMS BY LIGHT ISOTOPE NUCLEI

In the energy region  $-\frac{1}{2}Af \in E' \in \frac{1}{2}AE$  when the concentration of the heavy hydrogen isotope is small the most essential process is an elastic scattering of heavy mesic atoms by light isotope suclei and further after mesic atom slowing down -formation of mesic molecules.

Let the solutions obtained by numerical integration of (21) with boundary conditions (33) and (34) respectively for  $R \rightarrow \infty$  take the form:

$$a_{b}^{(1)}(R) \approx d_{b,}^{(2)} e^{-R_{a}R_{a}} + d_{b_{2}}^{(1)} e^{R_{a}R_{a}}; \quad a_{b}^{(2)}(R) \approx d_{b_{a}}^{(2)} e^{-R_{a}R_{a}} + d_{b_{2}}e^{H_{a}R_{a}}$$

$$b_{b}^{(1)}(R) \approx d_{b_{a}}^{(1)} \sin\left(H_{a}R - \frac{F_{b}}{2} + \omega^{(1)}\right); \quad b_{b}^{(2)}(R) \approx d_{b}^{(2)} \sin\left(H_{a}R - \frac{F_{b}}{2} + \omega^{(2)}\right)$$

$$(47)$$

Forming the linear combination from (47) satisfying the condition (26) we obtain within the accuracy of constant factor

$$\delta_{\nu}(2) \approx \sin(il_{2} 2 - \frac{\pi L}{2} + \omega)$$
  $a_{\nu}(2) \approx \frac{d_{\nu}^{n} d_{\nu a}^{(2)} - d_{\nu a}^{n} d_{\nu a}^{(2)}}{T} e^{-2i2}$  (46)

$$d_{\mu} = \frac{d_{\mu_1} \cdot d_{\mu_2} \sin \omega'' - d_{\mu_1} d_{\mu_2} \sin \omega'^{(2)}}{d_{\mu_2}^{(2)} \cdot d_{\mu_2}^{(2)} \cos \omega'' - d_{\mu_1}^{(2)} d_{\mu_2}^{(2)} \cdot \cos \omega'^{(2)}};$$

Partial cross section corresponding to the L wave in

$$\frac{1}{\sqrt{2}} (2L+1) \sin^2 \theta = \frac{\sqrt{\pi}}{\sqrt{2}} (2L+1) \frac{\left[ d_{L_2}^{(4)} d_{L_2}^{(2)} \sin \theta - d_{L_3}^{(4)} d_{L_4}^{(4)} \sin \theta \right]}{T^2} d_{L_4}^{(4)} d_{L_5}^{(4)} d_{L_5}^{(4)}$$

the parties to know were functions and effective scattering cross section when the kinnergy of sections is small (  $N_2 \ll l$  ). In the region  $R_0 \ll R \ll \frac{l}{l}$  , the solutions (4) for the very may be represented in the form:

The Major condition (61) entirelying the condition (26) in the region  $R_i = R = \frac{1}{2}$  to of the lines

$$2 = \frac{3^{1/2} - 3^{1/2}}{3^{1/2} - 3^{1/2}}; \qquad (52)$$

The constitution of the functions (III) is shown so that by  $R \to \infty$  it corresponds to a chap wave of the telephone matter of material (with coefficient 3) and to a moves that is near a could work to Table Y the wave functions of (III) and \$(IV) for the systems proton-like materials and decomparations are given. The effective cross section of economy of the function of the part wave at small bisatic energy of small areas.

$$\frac{g^{-1}}{a^{-1}} - \frac{g^{-1}}{a^{-1}} - \frac{g^$$

The relieue Am Command Am are given in Table II. Note that in the case of the process of the process of the process of the factorial in 718/.

The relieue of the relieue of the sharp containing may be a small of the charge containing may be a small of the charge containing may

where  $N = \frac{4}{M_{\star} + M_{\star}} = \frac{4}{3}$  is the mean value of the energy transmitted in  $d_{\mu} + P$  collision  $N = 4 \cdot 10^{22}$  E= 45 eV is the energy acquired by the mesic atom  $d_{\mu}$  while charge exchanging  $E_{\chi} \sim 2.10^{-4} eV$  is the final energy. (In this case we make the rough approximation that  $d_{\mu}$  is believed to move along a straight line since the deviation of  $d_{\mu}$  in cultision with proton can not exceed 30° in the laboratory system of coordinates). The value of the free path according to (54) is  $\ell \sim 0.1$  mm. (The free path owing to the diffusion of  $d_{\mu}$  with the thermal energy is also of order of 0.1 mm) which is applying less than the experimental 'hole' of about 1 mm.

### MESIC MOLECULE ENERGY LEVELS

Let in the energy region  $E' \leftarrow \frac{1}{2} \Delta E$  the solutions of Eq. (21) under the initial conditions (33) and (34) correspondingly have for  $R \rightarrow \infty$  the following form:

$$Q_{i}(R) \approx \mathcal{I}_{i}^{(i)}(E')e^{-R_{i}R} + \mathcal{I}_{2}^{(i)}(E')e^{-R_{i}R}$$

$$\theta_{i}(R) \approx \mathcal{I}_{3}^{(i)}(E')e^{-R_{i}R} + \mathcal{I}_{\gamma}^{(i)}(E')e^{R_{2}R}$$
(55)

Then, forming the linear combination the increasing exponents can be excluded only under the condition:

$$\left| \begin{array}{ccc} \mathcal{F}_{2}^{(\prime)}(E') & \mathcal{F}_{2}^{(\omega)}(E') \\ \mathcal{F}_{y}^{(\prime)}(E') & \mathcal{F}_{y}^{2}(E') \end{array} \right| = 0$$
(56)

The condition (56) determines mesic molecule energy levels. By means of the numerical integration of the system (21) for various E' we can choose the values of E' satisfying the condition (56). The mesic molecule energy levels obtained in such a way are given in Table III. In Fig. 1 the values of the functions a ( $\mathcal{R}$ ) and b ( $\mathcal{R}$ ) are given for the bound state of the mesic molecule (pt) an ormalized by the condition

$$\int \left( \left| a(R) \right|^2 + \left| b(R) \right|^2 dR = 1$$
 (57)

#### SMERGY LEVELS OF MESIC MOLECULES WITH IDENTICAL NUCLEI

As we have already pointed out the system for the mesic molecules with identical nuclei breaks up two independent equations. The effective potentials of interaction with corrections taking into account the motion of nuclei\*  $\ell g + \frac{1}{2M_{\rm He}} \kappa' gg$  are approximated with a good accuracy by the well-known Morse function:

$$U = A \left[ e^{-2A(R-R_0)} - 2e^{-A(R-R_0)} \right]$$
 (58)

The values of the effective potentials of interaction are given in  $^{13}$ . The deviations from the Morse function from the true values of effective potentials of interaction can not change considerably the value of the levels since these deviations are appreciable only in those regions (for very large or very small  $\mathcal L$ ) where the wave functions decrease exponentially. The values of the energy levels are given in Table III.

# SCATTERING OF MESIC ATOMS BY MUCLEI IDENTICAL TO THE MESIC ATOM MUCLEUS

For small energy of the relative motion of  $(R'R \ll 1)$  it is not difficult to calculate effective cross section of mesic atom scattering by suclei of the isotope\*\*. For E' > 0 the solution of the Schredinger equation with potential (58) is of the form

<sup>\*</sup> Compare with '14', where the approximation was performed without taking into account the corrections to the metion of musici.

The easery of the relative motion must be considerably higher than the energy of the superfine spiliting in the means of the means atom P. It is about of 0.2 ev). The effects at lower energy are considered in ...

$$3 = \frac{2\sqrt{MA}}{d}$$
  $= \frac{\sqrt{2ME'}}{d} = \frac{R}{d}$ ;  $e^{i\phi} = \frac{\Gamma(1+2i\pi)\Gamma(-\frac{\sqrt{2MA'}}{d} + \frac{1}{2} - i\pi)}{\Gamma(1-2i\pi)\Gamma(-\frac{\sqrt{2MA'}}{d} + \frac{1}{2} + i\pi)}$ 

For  $\mathcal{R} \rightarrow \infty (\xi \rightarrow 0)$  this solution equals asymptotically:

$$g = \sin\left(k2 - \frac{\kappa \ln 2\sqrt{\frac{2MA}{A}}}{d} - \kappa R_{\bullet} + \varphi\right) \tag{60}$$

If the energy of the relative motion is rather small (#  $R_o \ll 1$ ) then, in the region  $R \ll R \ll \frac{1}{2}$ 

$$g \sim R - \lambda g \tag{61}$$

The scattering length may be obtained from (64),(65)

$$\lambda_{g} = \left( \psi \left( -\frac{\sqrt{2MA}}{d} + \frac{1}{2} \right) - 2\psi(1) + \ln \frac{2\sqrt{2MA}}{d} \right) \frac{\lambda}{2MA} + R_{o}$$
(62)

where  $\psi(x) \cdot \frac{\Gamma(x)}{\Gamma(0)}$  is

(real or virtual with the energy close to zero) then, due to the fact that the function  $\psi(z)$  has poles for integer negative numbers I the value of Ag may be very large. The possibility

of such a resonance has been observed in  $\frac{2}{.}$ 

The solution of the second equation (21) may be also obtained easily if the potential is approximated by an exponent: Vu = [E' (R) + 1/2H. K' (R)] (63)

Vu = 80-69

this may be made with a good accuracy for the values of R essential for the scattering. The Schrödinger equation with potential (63) reduces to the Bessel equation of the imaginary argume by introducing a new variable quantity. Thus, for E' = 0

where Ka(t) is the Hankel function of the imaginary argument. The normalization of the funcis chosen so that for R- - the solution will be of the form:

(taking into account that for  $t \to 0$ ,  $K_0(t) + \ln \frac{\lambda}{h} - C$  where C = 0.577 is the Euler constant) we obtain  $\lambda_u = \frac{2}{\beta} \left[ c + \ln \frac{\sqrt{2MB}}{B} \right]. \tag{65}$ 

Taking into account that the mesonic function  $\mathcal{L}_g(\overline{t},R)$  is symmetrical with respect to the nuclium exchange and  $\mathcal{L}_g(\overline{t},R)$  is antisymmetrical, it may be concluded that in the S- wave the relative motion of identical nuclei will be described by the function g(R), if the summary spin of nuclei is odd. The affective excess section of the hydrogen mesic atom scattering by protons (and mesic atoms of tritium by tittium satisfie) at small energies is to be of the form:

$$5 = 2\pi \left( \frac{\lambda_0^2}{4 + \frac{\lambda_0^2}{1 + \frac{\lambda^2}{4}}} + \frac{3}{4} + \frac{\lambda_0^2}{1 + \frac{\lambda^2}{4} + \frac{\lambda^2}{4}} \right)$$
 (66)

and the second of most branch of Betterium by Conterous:

$$6 = 2\pi \left( \frac{2}{3} \frac{\lambda_0^2}{1 + N^2 \lambda_0^2} + \frac{1}{3} \frac{\lambda_u^2}{1 + N^2 \lambda_u^2} \right). \tag{67}$$

The formula (66) is easiogous to that describing the scattering of seutrons by protons. For large is accordance with (66) there will be a resonance in the scattering when  $\mathcal{K} \longrightarrow 0$ .

The sales of the second control of

#### MESIC HOLECULE FORMATION

Moving in the matter the hydrogen mesic atoms in virtue of their neutrality can go easily through the electronic shells of the hydrogen molecules and approaching the nuclei they can form mesic molecules (more exactly, mesic molecular ions)  $(PP)_{\mu}^{*}$ ,  $(PQ)_{\mu}^{*}$  etc. (like the exactly mesic molecular ions)  $(PP)_{\mu}^{*}$ ,  $(PQ)_{\mu}^{*}$  etc. (like the exactly mesic molecule, if principle, may be transmitted to the radiation, electron shell and to the nucleus coupled by

chemical forces with that which forms the mesic molecule.

The last transition, however, may have some meaning only in the case when the mesic molocule forms itself in the state with very small coupling energy (of order of the coupling energy of the ordinary molecule). As we can see from Table III this condition can not be fulfilled for any of the molecules (perhaps, except for (dd), ). Since the size of the mesic molecule is been then the atomic one the relations between the probabilities of formation of a mesic molecule in a radiation way and by means of the recoil of the energy to the electron of the shell may be expresent using the standard theory of intrinsic conversion of electrons under nuclear transitions. in the considered region of transmitted energies (tens -hundreds of ev) the coefficients of intrinair conversion are very large; therefore the probability of the radiative formation of mesic molecules is less incomparably than the conversional one. Because the formation of mesic molecules takes place at small relative energies of mesic atoms an electric dipole transition from the S wave of continuous spectrum with the conversion on electron will be the most important one. Let he distances from the nuclei M, M2 respectively from an arbitrary point; then the Coulomb field of the system at large distances has the

$$\frac{f}{f_0} + \frac{f}{f_0} - \frac{f}{f_0} \approx \frac{f}{f} + \frac{df}{f^2} \tag{68}$$

where I is the distance from the center of meas of nuclei, and d is the dipole momentum of

$$\vec{d} \cdot \vec{z} \frac{M_A \cdot M_I}{M_A \cdot M_I} \vec{R} - \frac{1}{\lambda} (\vec{z}_1 + \vec{z}_2)$$

$$(\vec{R} \cdot \vec{Z}_2 - \vec{Z}_1; \vec{z}_1 \cdot \vec{z} - \vec{Z}_1; \vec{z}_2 \cdot \vec{z} - \vec{Z}_2). \tag{60}$$

If this procles Coulomb functions of the hydrogen atom are taken as wave functions of electren them in acclugy with the probability of conversion under the auclear transition we obtain for the probability of made melecule formation by means of disple conversion:

$$W = \frac{16}{3} \frac{25\% e^{-4\pi a \kappa r d} g^{2}}{(10)^{2} (10)} \sum_{N_{0}} |\langle d \rangle|^{2}.$$
 (70)

If  $A_{ij} = A_{ij} = A_{ij}$  and velocity),  $A_{ij} = A_{ij} = A$ 

decrete spectrum respectively.

(1) is performed over the coordinates of M -meson and smolel). The inte-

$$d_{y_0} \cdot \int Z_g \frac{1}{2} (\tau_1 + \tau_2) Z_{\nu} (dz_{\mu})$$
 (72)

Facilities released symmetry it is clear that dgu is directed along R: dge f (RIR, where

The acceptance [EAS Sales for small R, however, it is river that since the function [EAS Sales for small values of R vanishes exponentially the small R too, if the calculation of of gay is made the small small resolution of the small possible final senses the small resolution in [70] is made over all possible final senses the small resolution in the continues specifies and is simulated to be chosen so that at the infinity there a plane wavewith the coefficient one, and was binaries of the discrete spectrum is, sormalized to unity. In this case the matrix element is well have the discrete spectrum is, sormalized to unity. In this case the matrix element is well have the discrete apactrum is, sormalized to unity. In this case the matrix element is well have the discrete apactrum is, sormalized to unity. In this case the matrix element is a content to rewrite the fermula (70) in the form

$$W = \frac{16}{3} \left( Md_e^2 \right) \left( \frac{m_e}{m_{ph}} \right)^5 \frac{e^2}{10e} \frac{2\pi l^2 e^{-4e \cos(\frac{l}{2}\theta)} \left( \frac{5}{l^2} \left| cd \right|^2 \right)}{10e^{-2\pi l} \left( l^2 e^{-2\pi l} \right) \left( l^2 e^{-2\pi l} \right)}, \tag{74}$$

where the metrix element  $\langle d \rangle$  is calculated in dimensionless ('mesic stom') units. It is easy to see that the first term in the dipole momentum (69) has non-zero matrix elements only for transitions with mesonic functions of identical parity  $Z_g - Z_g$ ;  $Z_u - Z_u$  while the second term gives transitions only between mesonic functions of different parity ( $Z_u - Z_g$ ;  $Z_u - Z_u$ ). The dipole transitions from the S-wave of the continuous spectrum may occur only into the resultion state with L = 1. From the table III one can see that for all mesic molecular terms ( $L_u - L_g$ ) the transition is performed into the ground rotation state (L = 1; R = 0). For most molecules  $L_g - L_g$ ) the transition into the vibration-rotational state is possible too.

liky of formation of mesic molecules with identical nuclei 4 = 1; n = 1 may be callegansity as it was made for mesic molecules in (dd), The probabilities of formation of hase applications are given in the Table 4. In the case of mesic molecules with different nuclei of nates interest in the calculation of probability of mesic molecule formation when the collision the maste atom of bravier leatops with lighter nucleus occurs, for example  $d_{\mu} + p \rightarrow (dp)_{\mu}$ the collection part d the charge exchange is the most probable process product p). es of the initial state has the form:

To To are connected with the functions Q.R.), L(R) e of the final state corresponding to the retation level of the meals

$$\{(0, \psi)_{n+1}, (\psi)_{n+1}\} \cdot \frac{1}{2} Y_{q,n} (\theta, \psi). \tag{76}$$

(common to large N.

(control) \*\* (e\*\*,e\*\*)

(control) \*\* (e\*\*,e\*\*) (LC10)

(control) \*\* (e\*\*,e\*\*) (LC10)

(control) \*\* (e\*\*,e\*\*) (LC10)

D.2.

(MA ) consistent for small R, when Zg and Zu treasform rec-

positively into is and 20 levels of He.

$$\Sigma_{u} = -\frac{1}{N_{0}} e^{-(z_{1} + z_{2})}$$

$$\Sigma_{u} = -\frac{1}{N_{0}} e^{-iz_{2}(z_{1} + z_{2})} (z_{1} \cos \theta_{1} - z_{2} \cos \theta_{2})$$

$$N_{0}^{2} = \frac{\pi}{N_{0}} e^{-2z_{1}} (1 + 2z_{2} + \frac{\pi}{N_{0}} z_{2}^{2})$$
D.4

$$N_{4}^{2} = 4\pi \left(1 + R + \frac{9}{20}R^{2} + \frac{7}{60}R^{3} + \frac{7}{60}R^{7}\right)e^{-R}$$
D.4'

in the approximation (LCAO):

$$k_{99} = \frac{1}{2} - \frac{s}{2(1+2)} - \frac{1}{36} \frac{2^2(1+2)^2}{(1-5)^2} e^{-2\pi}$$
D.5

$$N_{uu} = \frac{1}{2} + \frac{S}{2(1-3)} - \frac{1}{36} \frac{\pi^{2}(1+\pi)^{2}}{(1-3)^{2}} \cdot e^{-2\pi}$$
D.5'

In the appreximation (U . A ):

$$R_{gg} = 1 - \left(\frac{M_0^2}{M_0^2}\right)^2 \approx_{R \to 0} 1 - \frac{16}{9} R^2$$
 D.6

$$M_{UU} = \frac{2}{\sqrt{2}} + \frac{1}{\sqrt{4}} - \left(\frac{N'U}{N'U}\right)^2_{R \to 0} = \frac{2}{9^2} + \frac{1}{4}$$
 D.6

For comparison in Fig. 2,3 are given the values K gg and K uu , calculated in  $^{/15/}$  and according to the approximation (LCAO) and (U . A) . For the value Q(R) we get:

$$(L(40)Q = -\frac{M_A - M_1}{M_A + M_1} \cdot \frac{R(R+1)e^{-R}}{6\sqrt{1-\hat{S}^2}}$$

We note that Q calculated in accordance with (LCAO) for  $R \rightarrow 0$  coincide well with the values of Q, calculated in accordance with

$$\left( L(A0) \begin{cases} \log \frac{1}{2\sqrt{1-3}} & \left( 1+e^{-R} \left( 1+R-\frac{R^2}{3} \right) - \frac{R^2(1+R)^2 - 2R}{9(1-S)} e^{-2R} \right) \frac{M_2 - M_1}{M_2 - M_1} \\ \log \frac{1}{2\sqrt{1-3^2}} & \left( 1-e^{-R} \left( 1+R-\frac{R^2}{3} \right) - \frac{R^2(1+R)^2}{-9(1+S)} e^{-2R} \right) \frac{M_2 - M_1}{M_2 + M_1}$$

Thus, in the all region  $\mathcal{R}$  the approximation Q = QLCAO may be taken.

Kgu (R) and Kug(R) in the approximation (LCAO) and (UA) equal cor-

(U A) 
$$\begin{cases} M_{g0} = \frac{M_{g} - M_{1}}{M_{g} + M_{1}} \cdot \frac{64\pi}{81} \cdot \frac{e^{-3\frac{\pi}{12}}}{M_{g}N_{3}} \left(1 + \frac{3}{2}R + \frac{3}{4}R^{2}\right) \left(1 - \frac{R}{2} \frac{N_{3}}{N_{3}}\right) \frac{1}{R} \\ M_{3}^{2} = \frac{M_{g} - M_{1}}{M_{g} + M_{1}} \cdot \frac{64\pi}{81} \cdot \frac{e^{-2R_{2}}}{M_{g}M_{3}} \left(\frac{1}{2} \frac{N_{2}^{2}}{M_{3}} (1 + \frac{3}{2}R + \frac{4}{2}R + \frac{4}{2}R^{2}) + \frac{3}{2}R + \frac{4}{16}R^{2}\right) \\ + \frac{3}{2}R + \frac{4}{16}R^{2}\right). \end{cases}$$

Show the behaviour of the function for 
$$R \rightarrow 0$$
.

 $R_{gu} = (L(10) \rightarrow \frac{M_0 - M_1}{M_0 + M_1}, \frac{2}{\sqrt{3} \cdot R} \approx 1,15 \frac{1}{R}, \frac{M_0 - M_1}{M_0 + M_1}, \frac{2}{\sqrt{3} \cdot R} \approx 1,15 \frac{1}{R}$ 

$$Rag(UJ) \rightarrow \frac{N_2-N_1}{N_2+N_1} \frac{8\sqrt{\Sigma}}{55} R \approx 0.528 \frac{N_2-N_1}{N_2+N_1}$$

T a b i e I charge exchange cross section

	P,+d +d, 1P	Pm+1-+tm+P	$d_{\mu} + t \rightarrow t_{\mu} + d$
f	2.1	0.84	0.0067
64.V	3.42 . 10 <sup>-13</sup> cm² sec	1.49 10-13 cm² sed	1.15 . 10 <sup>-15</sup> cm <sup>3</sup>
би	$1.98 \cdot 10^{-19}  \mathrm{cm}^2$	1.53 · 10 <sup>19</sup> cm <sup>2</sup>	2.41 . 10 <sup>-19</sup> cm <sup>3</sup>

T a b l e II mesic atom elastic scattering cross section

	dy+P - dy+P	$t_n + p \rightarrow t_n + p$	$t_{j_1}+d \rightarrow t_{j_2}+d$
λ	2.03	2.66*	6.7
6,00)	3.39 . 10-20 cm <sup>2</sup>	5.84 . 10-20 cm2**	36.9 . 10-20 cm <sup>2</sup>

T a b l e 111

mesic molecule levels (ev) (for mesic molecules with various nuclei the energy levels are calculated from the level of heavier isotope)

		L.O	۷	• 0	L=2	L:3
	n = 0	n= 1	n = 0	. n = 1	n= 0	n= 0
( pp )	252		109			•
( 99 ),	330	40	227	7?	88	-
( tt )*	367	86	283	45	170	50
(pd)*	220	-	90			
(pt);	213		93	-		-
(dt);	318	32	232		102	-

<sup>\* \*\*</sup> These values are derived for Kek 2 0. Calculations with correct value of Kes give for A the value ~ 10. what seems to be doubtful.

T a b l e lV probabilities of mesic molecule formation in units  $10^6~{\rm sec}^{-1}$  in liquid hydrogen

( pp )	( dd )*	( tt ),	( pd ),	$(-\mathrm{d} t)_{\mu}^{\star}$	( pt )*
1.53	0.006	0.38	0.7	~0.001	0.25

In the present paper the probabilities of the mesic molecule formation schould be considered to be correct only in order of value, since the binding of hydrogen nuclei in molecules of H<sub>2</sub> has been neglected in our calculations what leads apparetly to the increase of W.

In the case of the mesic molecular ion (dd) and (dt) 0-0 transitions may contribute to the molecule formation probability, due to the oscillation level close to zero (L=0).

We have just reseived preprints by Cohen, Judd and Riddell. They calkulate the probability of the formation of mesic molecules with identical nuclei using the wave functions normalised to \$\sqrt{2}\$, but not to unity, what doubles the value of \$W\$.

We wish to thank Y.B. Zeldovich for initiating this investigation and for many useful discussions.

Table (

functions of mesic polecular ions (unnormalized) in state L = 1

<del>*************************************</del>		() (1)	•	(dt	) •	
مراهم)		Tevel 9	d#		23? ev	
Level 90	) <b>ev</b>	10 45 L 20	• •.•.		-	
	*					<b>A</b>
* 1 o(R)	b(R)	a(R)	b(ii)	a(H)	b(R)	R
	0,110 10-	.0,116 10-2	$0,109 \cdot 10^{-2}$	+0,772 10-3	+0,823 10-3	0,3
0,3 0,114 10-2	0,516 10	0,554 10 <sup>-2</sup>	0,531 10-2	0,427 10-2	0,420 10-2	0,5
0,5 6,536 10-2	0,130 10-1	0,141 10 <sup>-1</sup>	0,137 10-1	0,122 10-1	0,121 10-1	0,7
0,7 0,132 10-1	0,130 10	$0.277 \cdot 10^{-1}$	0,273 10-1	0,246 10-1	0,260 10-1	0,9
0,9 0,256 10-1	$0,254   10^{-1}$ $0,424   10^{-1}$	0,462 10-1	0,462 10-1	0,464 10-1	0,462.10-1	1,1
1,1 0,423 10-1	0,632 10-1	0,687 10	0,697 10-1	0,718 10 <sup>-1</sup>	0,719 10-1	1,3
1,3 0,625 10-1	0,032.10	0,936 10	0,904 10-1	0,100	0,101	1,5
1,5 0,849 10-1	0,869 10-1	0,956 10	0,125	0,129	0,131	1,7
6,7 *Quality	0,110		0,157	0,196	0/279 m	
1,9 0,130	0,137	0,144	0,179	0,179	0,183	2,1
2,1 0,151	0,160	0,165	0,202	0,196	0,202	2,3
2,3 0,166	0,181	0,183	0,221	0,207	0,214	2,5
2,9 0,162	0,198	0,197	0,235	0,213	0,219	2,7
2,7 0,191	0,211	0,206 0,210	0,245	0,210	0,219	2,9
2,9 0,197	0,221	0,210	0,250	0,203	0,213	3,1
3,1 0,196	0,226	0,210	0,293	0,193	0,204	3,3
3,3 0,196	0,228	0,198	0,249	0,179	0,191	3,5
),5 0,191	The second secon	0,189	0, 43	0,104	0,176	3,7
3,7 0,184	0,221	0,187	0,234	0,148	0,160	3,9
3,9 6,179	0,215	0,177	0,224	0,131	0,143	4,1
4,1 0,164	0,200	0,151	0,212	0,115	0,127	4,5
4,3 0,152	0,184	0,137	0,200	0,100	0,111	4,5
4,5 0,140	0,173	0,124	0,187	0,866 10-1	0,969 10-1	479
4,7 0,126 4,9 0,116	0,161	0,111	0,173	0,741 10-1	0,838 10-1	4,9
7,1 0,104	0,149	0,989 10-1	0,161	0,630 10 <sup>-1</sup>	0,719 10-1	5,1
9,3 0,935 10 <sup>-1</sup>	0,137	0,875 10-1	ú,148	0,532 10	0,614 10-1	5,3
5,5 0,833 10 <sup>-1</sup>	0,176	0,770 10-1	.0,136	0,447 10-1	0,521 10-1	5,5
2,7 0,730 10 <sup>-1</sup>	0,115	0,673 10-1	0,125	0,373 10-1	0,440 10-1	5.7
5,9 0,650 10 <sup>-1</sup>	0,105	0,585 10-1	0,114	0,310 10-1	0,371 10-1	5,9
6,0 0,609 10-1	0,100	0,545 10-1	0.109	0,283 10-1	0,340 10 <sup>-1</sup>	6,0
6,2 0,534 10-1	0,908 10-1	-0,471 10 <sup>-1</sup>	- 0,993 <b>10<sup>-1</sup></b>	0,233 10 <sup>-1</sup>	0,279 10-1	o•2."
6,4 0,465 10-1	0,822 10-1	0,401 10-1	0,905 10 <sup>-1</sup>	0,193 10-1	0.237 10-1	6,4
6,6 0,403 10-1	0,742 10-1	0.34: 10-1	$-0.823  10^{-1}$	0,158 10-1	0,197 10-1	6,5
6,8 0,348 10 <sup>-1</sup>	0,669 10-1	0,290 10	0,749 10	0,129 10	0,164 10	6,8
7,0 0,299 10-1	0,601 10-1	0,24% 10	_ 0,681 10 <sup>-1.</sup>	0,106 10-1	0,139 10	7,0
7,2 0,255 10-1	0,539 10-1	_0,198_1∂ <sup>=1</sup>	0,618 10 <sup>-1</sup>	. 0,865 10-2	0,111 10-1	7,2
7,4 0,216 10-1	0,483 10-1	0,158 10-1	ა,562 10 <sup>-1</sup>	0,701 10	0,910 10-1	7,4
7,6 0,181 10-1	0,432 10 <sup>-1</sup>	0,122 10 <sup>-1</sup>	6,511 10 <sup>-1</sup>	0,569 10 <sup>-2</sup>	0,738 10-2	7,6
7,8 0,150 10-1	0,385 10-1	0,835 197	0,454 10 <sup>-1</sup>	0,451 10-2	0,596 10-2	7,8
8.0 0.12, 10-1	0,342 10-1	0,557 10-2	$0,422 \cdot 10^{-1}$	0,381 10-2	0,478 10-2	8,0
8,5 0,677 10-?	$0,253 \cdot 10^{-1}$	0,136 10 <sup>-2</sup>	0,333 10-1	0,012 10 <sup>-2</sup>	0,253 10-2	8,5
and the second s						

dable V (constnuct.on)

Wave functions. Scattering of meric atom with a lawfor antope by nuclei of lighter one at some enemy

R	A(R)	<b>b(</b> R)	ر(۱)	<b>b(</b> f:)	3(P)	<b>b(</b> (;)).	
0,)	-0,469 10	-0,454 10	-0,10-10 <sup>-1</sup>		- 2, 1.4 10-2	-0,308 10 <sup>-1</sup>	P
0,5	-0,181 10 <sup>-1</sup>	-0,178 10 <sup>-1</sup>			-0, 382 10 <sup>-1</sup>	-0,377 10 <sup>-1</sup>	0,3
0,7	-0,386 10 <sup>-1</sup>	-0,382 10 <sup>-1</sup>		-0,935 10-1	-0,046 10 <sup>-1</sup>	$-0,939   10^{-1}$	0,5
0,9	-0,055 10 <sup>-1</sup>	-0,655 10 <sup>-1</sup>		-0,164	-0,178	-0,178	0,7
1,1	. <b>-0,9</b> 65 10 <sup>-1</sup>	-0,974 10 <sup>-1</sup>		-0,248	-0,281	-0,281	0,9
1,3	-0,129	-0,131	-0,329	-0,337	-0,337	-0,396	1,1
1,5	-0,159	-0,163	-0,407	-0,423	-0,477	-0,487	1,3
1,7	-0,183	-0,190	-0,470	-0,4,5	-0,540	-0,487	1,5
1,9	-0,201	-0,210	-0,513	-0,549	-0,560	-0,573	1,7
2,1	-0,210	-0,221	-0,532	-0,576	-0,533	-0,55	1,9
2,3	-0,210	-0,222	-0,526	-0,577	-0,452	-0,480	2,1
2,5	-0,202	-0,213	-0,498	-0,549	-0,353	-0,371	2,3
2,7	-0,186	-0,195	-0,449	-0,496	-0,217	-0,233	2,5
2,9	-0,163	-0,168	-0,385	-0,420	-0,661 10 <sup>-1</sup>	<b>-0,772</b> 10 <sup>-1</sup>	2,7
3,1	-0,137	-0,135	-0,310	-0,325	•	+0,847 10 <sup>-1</sup>	2,9
3,3	-0,107	-0,948 10 <sup>-1</sup>	-0,229	-0,215	0,239	0,242	3,1
3,5	-0,754 10-1	-0,508 10 <sup>-1</sup>	-0,145	-0,940 10-1	0,374	0,385	. 3,3
3,7	-0,440 10 <sup>-1</sup>	-0,378 10-2	$-9,631 10^{-1}$	+0,341 10-1	0,491	0,510	3,5
3,9	-0,136 10 <sup>-1</sup>	+0,451 10-1	+0,142 10-1	0,166	0,585	0,610	3,7
4,1	+0,148 10-1	0,948 10-1	0,849 10-1	0,299	0,655	0,685	3,9
4,3	0,407 10-1	0,145	0,147	0,431	0,703	0,734	4,1
4,5	0,636 10-1	0,194	0,201	0,561	0,729	0,757	4,3
4,7	0,832 10-1	0,242	0,245	0,687	0.737	0,757	5,3
4,9	0,996 10 <sup>-1</sup>	0,289	0,280	0,808	0.729	0,737	4,7
5,1	0,113	0,334	0,306	0,925	0,709	0,698	4,9
5,3	0,123	0,378	0,325	1,04	0,679	0,644	5,1
5,5	0,130	0,420	0,337	1,15	0,642	0,577	5,3
>,7	0,135	0,461	0,342	1,25	0,600	0,499	5,5
5,9	0,138	0,500	0,343	1,35	0,556	0,413	5,7
6,0	0,139	0,519	0,341	1,40	0,533	0,367	5,9
6.2	0.139	0.556	0.335	1.40	0.400	97701	6,0

1,49

1,58

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0,170

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0,836 10-1

0,571 10-1

0,176 10-1

0,122 10-1

0,834 10-2

0,388 10-2

0,385 10-1 -1,83

0,259 10-1 -2,11

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0,170

-0,151

-0,260

-0,374

-0,48

-0,593

-0,712

-0,994

-1,27

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-2,38

-2,06

-2,94

-3,49

0,653 10-1

 $-0,421 10^{-1}$ 

5,2

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Ú,8

7,0

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7.5

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8,0

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9,0

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10,5

11,0

11,5

12,0

13

0,139

0,137

0,134

0,130

0,126

0,121

0,115

0,110

0,104

0,981 10-1

0,844 10-1

0,724 10-1

0,523,10-1.

0,545 10-1

0,488 10<sup>-1</sup>

0,457 10-1

0,453 10-1

0,476 10-1

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12,0

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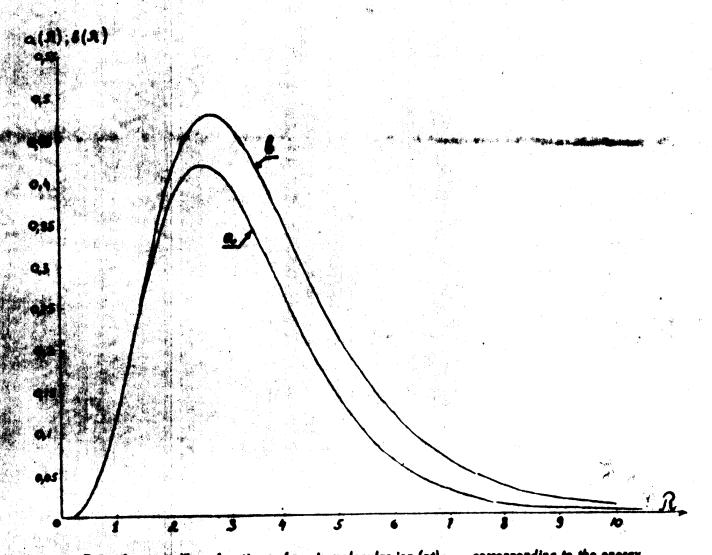
0,116

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Hove functions of mosts molecular ion (pt)... corresponding to the energy fixed 96 ov. The functions are given for illustration of qualitative behaviour of a (R) and 5 (R) for discrete values E. (Exact values of function are given to table Y).

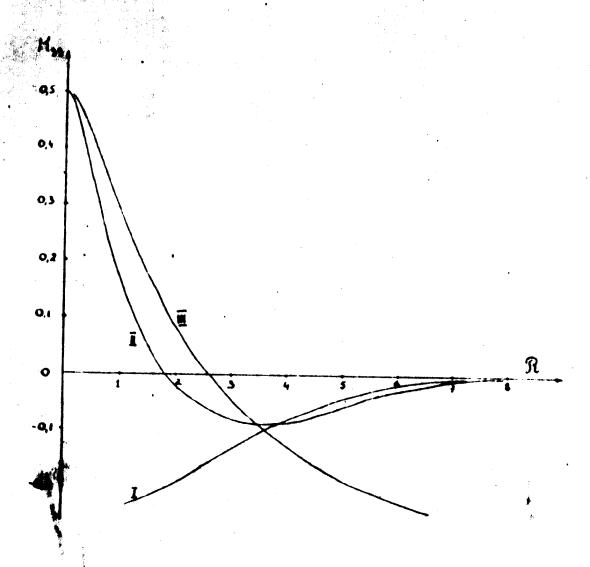


Fig. 2. Function Kgg calculated: I-in (LCAO)-approximation; II - with exact functions; III - in (UA) -approximation.

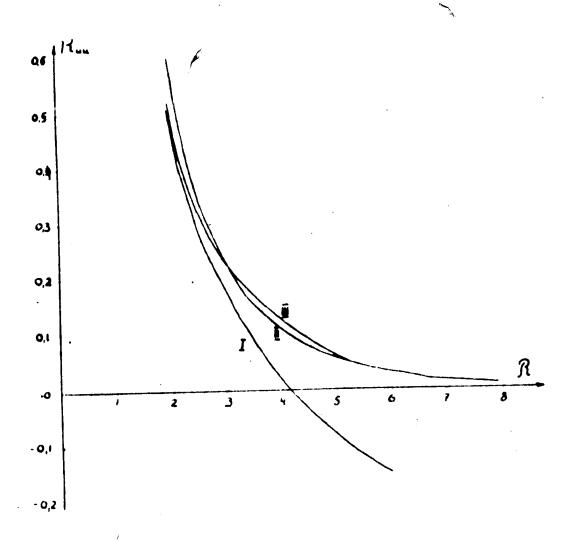


Fig. 3. Function Kuu calculated: 1-in (UA)-approximation; II-in (LCAO) approximation; III-with exact functions/15/.

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